

2.2 Separable Differential Equations

A first order DE is separable if it can be written as

$$\frac{dy}{dx} = f(x)g(y)$$

$$dy = f(x)(g(y))(dx)$$

$$\frac{dy}{g(y)} = f(x)dx$$

$$\int \frac{dy}{g(y)} = \int f(x)dx$$

Integration Techniques

* ① Parts

② Trig sub

* ③ Partial Fractions

* ④ u sub

⑤ Tables

* ⑥ Trig Functions

⑦ Series

Ex) 1

$$\frac{dz}{dx} = (x+1)^2$$

$$dz = (x+1)^2 dx$$

$$\int dz = \int (x+1)^2 dx$$

$$z = \frac{(x+1)^3}{3} + C$$

Ex) 2

$$\frac{dx}{dz} = (x+1)^2$$

$$dx = (x+1)^2 dz$$

$$\int (x+1)^2 dx = \int dz$$

$$\frac{(x+1)^3}{3} + C = z$$

$$z = \frac{-1}{(x+1)} + C$$